

## Chapter 20 Exercise Set A

- 1 population = box  
 population percentage =  $12,000 / 30,000 = 40\%$   
 sample = draws  
 sample size = 1,000  
 sample number = number of 1's among the draws  
 sample percentage =  $\frac{\text{sample number}}{\text{sample size}} \times 100\%$   
 denominator = 1,000

2a

2	3	}	400
1	0		

$EV_{\text{sum}} = .4 \times 400 = 160$   
 $SE_{\text{sum}} = .49 \times \sqrt{400} = 10$

box<sub>ave</sub> = .4    box<sub>sd</sub> = .49

2b

$EV_{\%} = 40\%$   
 $SE_{\%} = \frac{10}{400} \times 100\% = 2.5\%$

2c 40% give or take 2.5% or so.

3 percentage  $\rightarrow (50 / 10,000) \times 100\%$

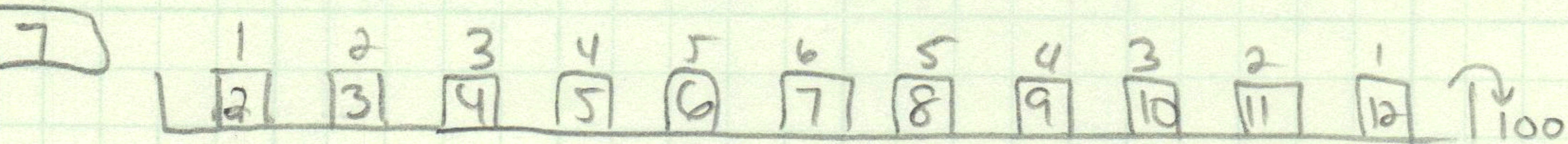
number of  $\rightarrow \sqrt{10,000} \times .5 = 50$

4a True box models are the same.

4b True there is a 1/4 chance of getting a 1.

5 False, they didn't change the box to 1/0.

6  $10\% + 1\% \rightarrow$  if you talk % stay in %.



box<sub>ave</sub> = 7  
 box<sub>sd</sub> = 2.42

$EV_{\text{sum}} = 7 \times 100 = 700$   
 $SE_{\text{sum}} = 2.42 \times \sqrt{100} = 24.2$

8 There always exists chance error! (HARD)



## Chapter 20 Exercise Set B

1a sample; population

1b number; percentage.

2a

$\text{box}_{\text{ave}} = .4$   
 $\text{box}_{\text{sd}} = .49$   
 $SE_{\text{sum}} = .49 \times \sqrt{1000} = 15.5$

$EV_{\%} = 40\%$   
 $SE_{\%} = (15.5/1,000) \times 100\% = 1.55\%$

2b 40% give or take 1.5% or so.

2c

$\frac{39-40}{1.5} = -.67$   
 $\frac{41-40}{1.5} = .67$   
 $\left. \begin{array}{l} \frac{39-40}{1.5} = -.67 \\ \frac{41-40}{1.5} = .67 \end{array} \right\} \underline{48.43\%} \text{ in middle}$

3a 100,000; one for every person in the population.

3b No; 1 if their income is  $> 75,000$ , 0 if their income is  $< 75,000$ .

3c

$\text{box}_{\text{ave}} = .2$   
 $\text{box}_{\text{sd}} = .4$   
 $SE_{\text{sum}} = .4 \times \sqrt{1600} = 16$

$EV_{\%} = 20\%$   
 $SE_{\%} = \frac{16}{1600} \times 100 = 1\%$

$\frac{39-40}{1} = -1$   
 $\frac{41-40}{1} = 1$   
 $\left. \begin{array}{l} \frac{39-40}{1} = -1 \\ \frac{41-40}{1} = 1 \end{array} \right\} \underline{68\%} \text{ in middle}$

4 The chance that we draw 22% or more persons with income over \$50,000.

5a The chance that 88 persons will have income over \$50,000

5b The chance the sample will have 22% earning  $> \$50,000$

5c No because % and sums are related.

$$\frac{88}{400} = 22\%$$



## Chapter 20 Exercise Set C

1 iii) They are both SRS so they are equally accurate.

2a  $\text{box}_{\text{ave}} = .5$   
 $\text{box}_{\text{SD}} = .5$        $SE_{\text{sum}} = .5 \times \sqrt{500} = 25$        $SE_{\%} = \frac{25}{2500} \times 100 = 1\%$

2b  $.5 \sqrt{25000} = 79 = SE_{\text{sum}}$        $SE_{\%} = (79 / 25000) \times 100\% = .31\%$

2c  $.5 \sqrt{100000} = 158 = SE_{\text{sum}}$        $SE_{\%} = (158 / 100,000) \times 100\% = .16\%$

3 if 20% 1's in box  $\rightarrow SD_{\text{box}} = .4$   
 if 40% 1's in box  $\rightarrow SD_{\text{box}} = .49$

if 20%  $\rightarrow SE_{\text{sum}} = .4 \times \sqrt{100} = 4$        $SE_{\%} = \frac{4}{100} \times 100 = 4\%$

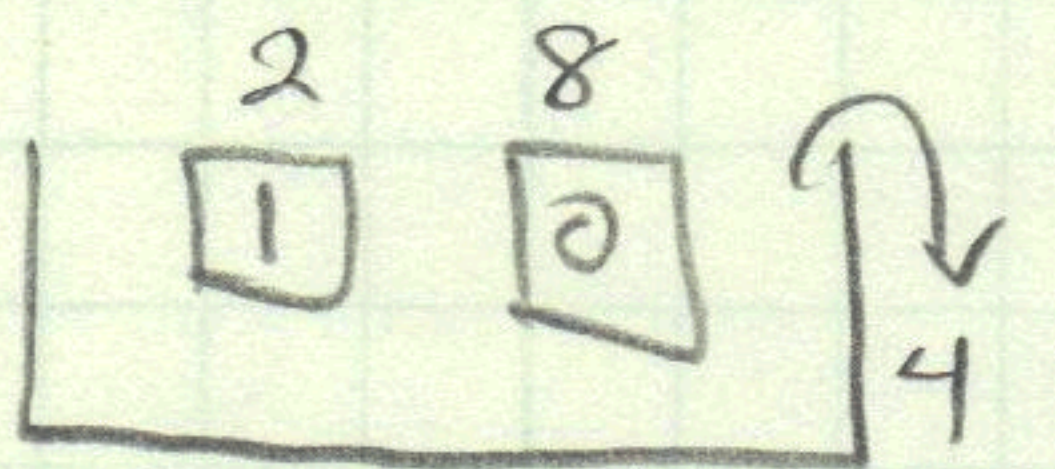
if 40%  $\rightarrow SE_{\text{sum}} = .49 \times \sqrt{100} = 5$        $SE_{\%} = \frac{5}{100} \times 100 = 5\%$

if 20%  $\rightarrow SE_{\text{sum}} = .4 \times \sqrt{2500} = 20$        $SE_{\%} = \frac{20}{2500} \times 100\% = .8\%$

if 40%  $\rightarrow SE_{\text{sum}} = .49 \times \sqrt{2500} = 24.5$        $SE_{\%} = \frac{24.5}{2500} \times 100\% = .98\%$

Choose 2500 draws!

4 Same, the proportions are all the same.

5 With:   $\text{box}_{\text{SD}} = .4$   
 $SE_{\text{sum}} = .4 \times \sqrt{4} = .8$        $SE_{\%} = \frac{.8}{4} \times 100\% = 20\%$

Without: In book.

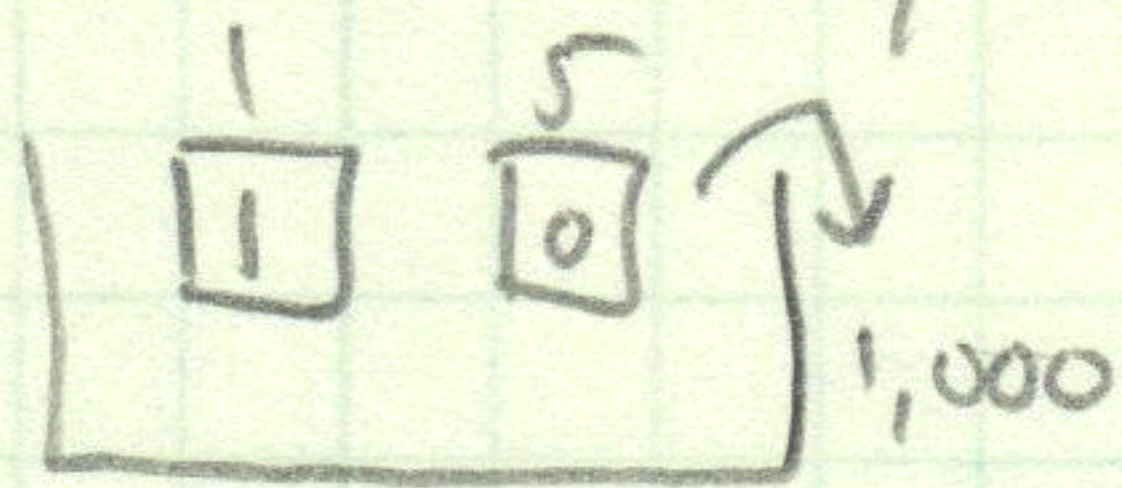
$$\sqrt{\frac{10-9}{10-1}} = \sqrt{\frac{6}{9}} = .82 \times 20\% = 16\%$$



## Chapter 20 Review Exercises

# tosses	$EV_{sum}$	$SE_{sum}$	$EV_{\%}$	$SE_{\%}$
100	50	5	50%	5%
2,500	1250	25	50%	1%
10,000	5,000	50	50%	.5%
1,000,000	500,000	500	50%	.05%

2 iii - Always set the box model first.



$$\begin{aligned} \text{box}_{ave} &= .167 \\ \text{box}_{sd} &= .37 \end{aligned}$$

$$\begin{aligned} EV_{\%} &= 16.67\% \\ SE_{\%} &= \frac{11.79}{1,000} \times 100 = \underline{1.179\%} \end{aligned}$$

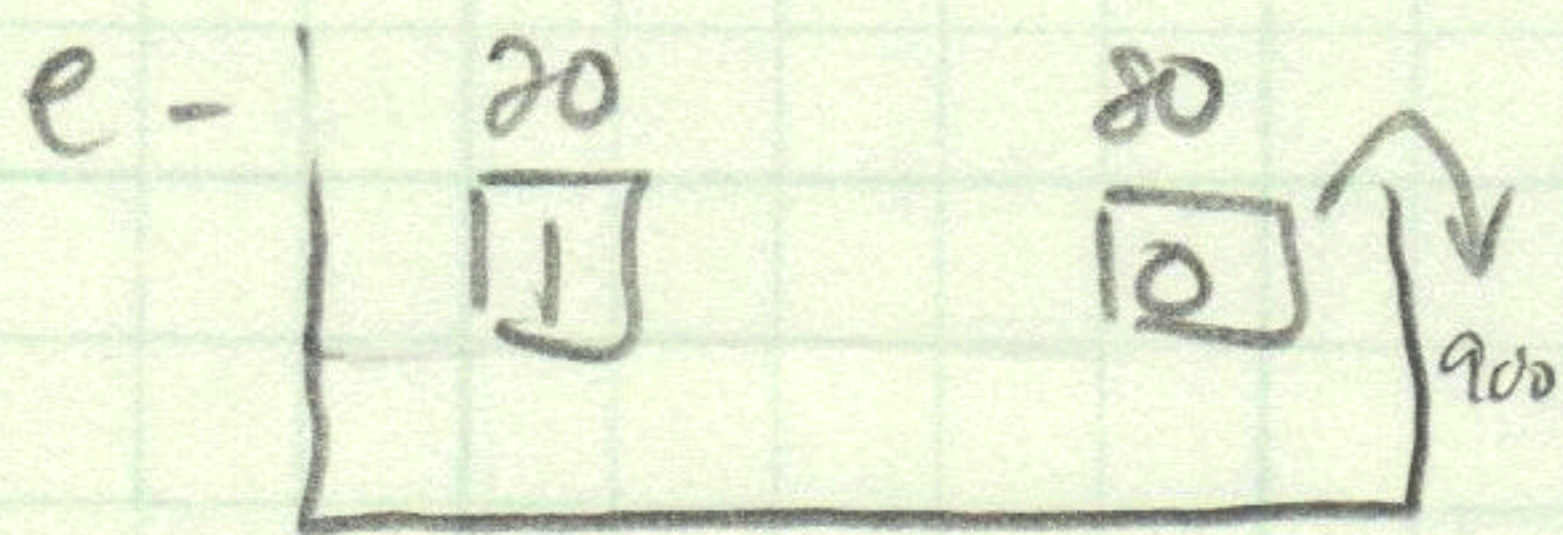
$$SE_{sum} = .37 \times \sqrt{1000} = 11.79$$

3 a- 50,000 one for each population member.

b- a zero or a one

c- False, it's a one/zero box.

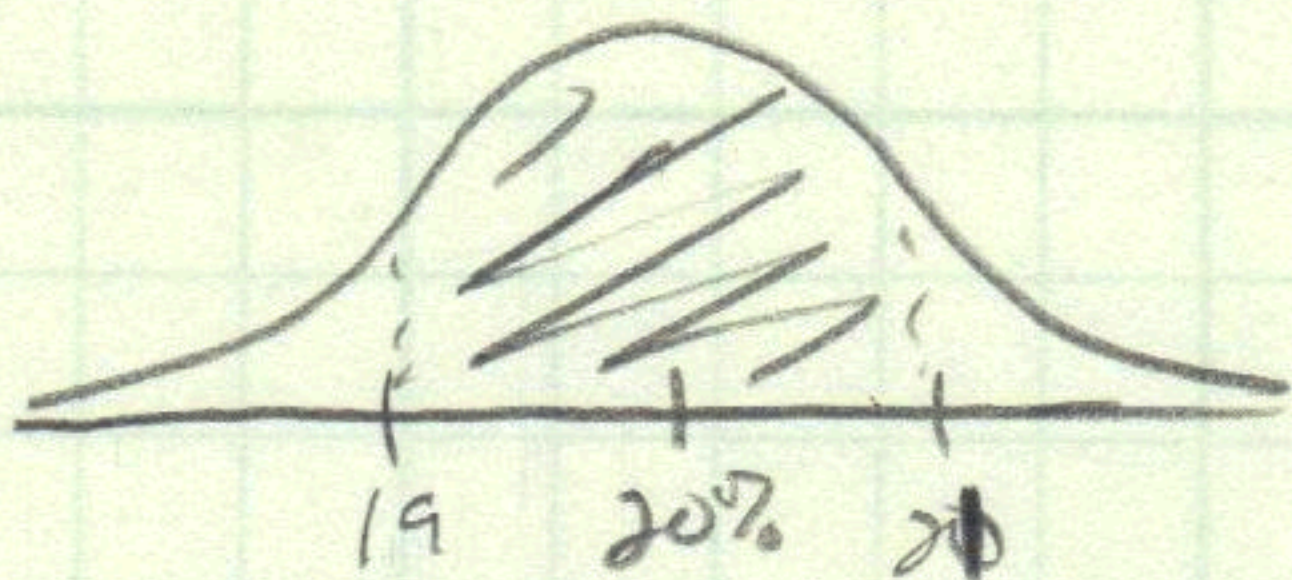
d- True.



$$\text{box}_{sd} = .4$$

$$SE_{\%} = .4 \times \sqrt{900} = 12$$

$$\begin{aligned} EV_{\%} &= 20\% \\ SE_{\%} &= (12/900) \times 100 = 1.33 \end{aligned}$$



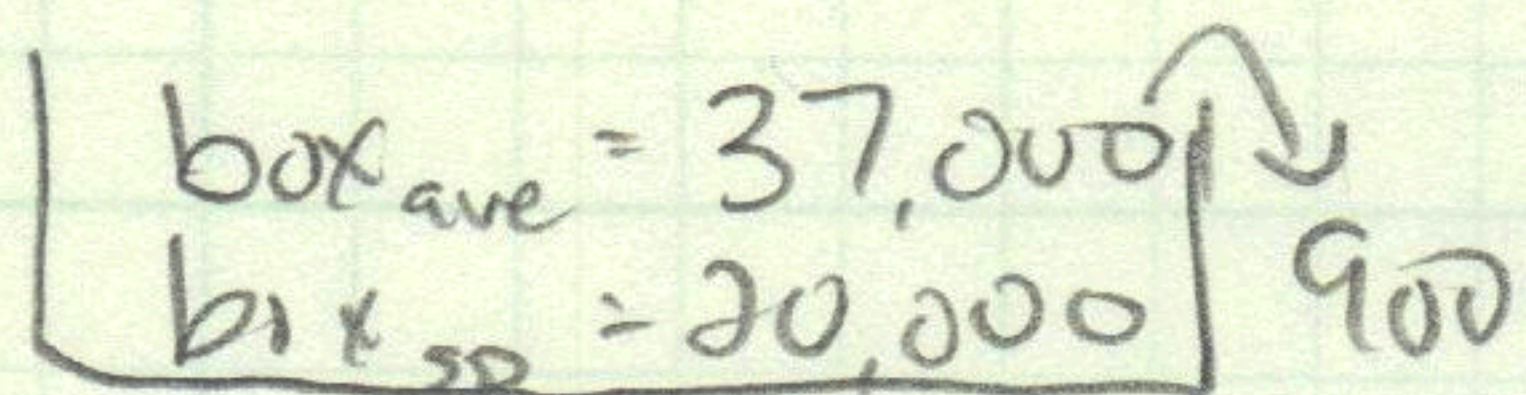
$$\frac{19-20}{1.33} = -.75$$

$$\frac{21-20}{1.33} = .75$$

54.67% in the middle

f- No, we don't have the percentages of incomes > 75,000.

4 TOTAL:



$$\begin{aligned} EV_{sum} &= 37,000 \times 900 = 33,300,000 \\ SE_{sum} &= 20,000 \times \sqrt{900} = 600,000 \end{aligned}$$

a- 50,000

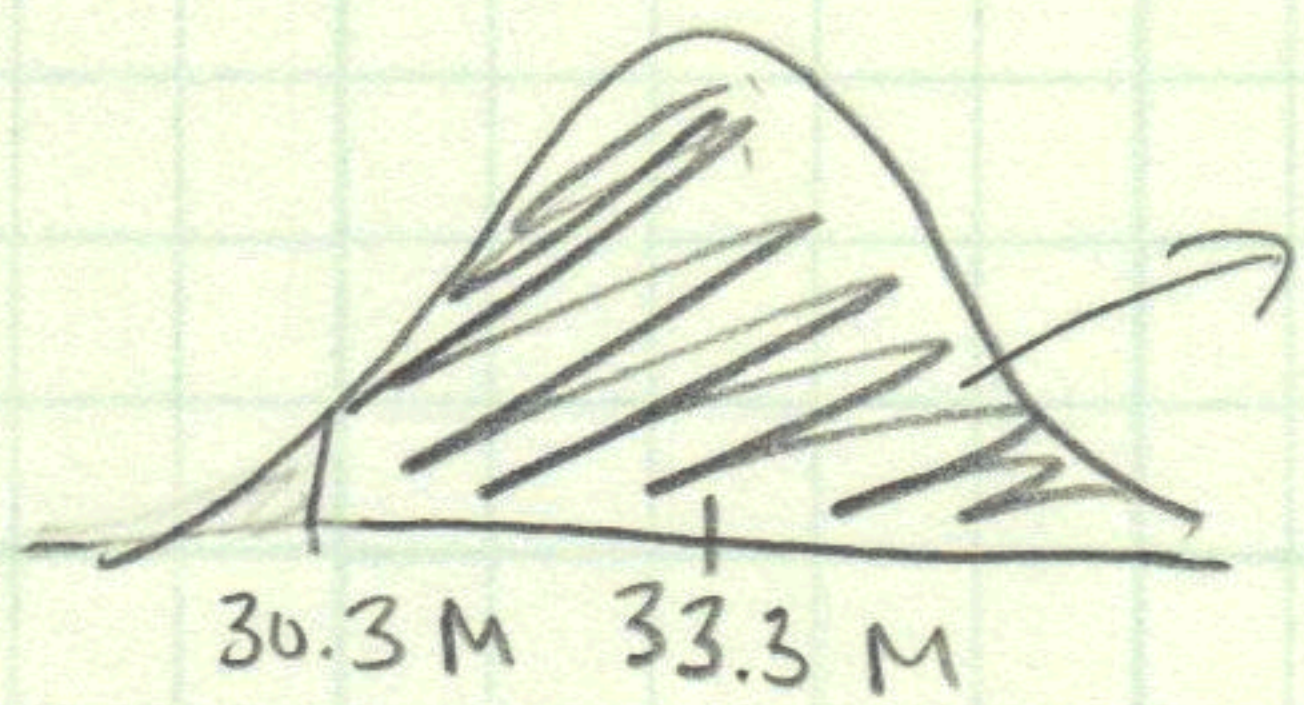
b- a gross income

c- True

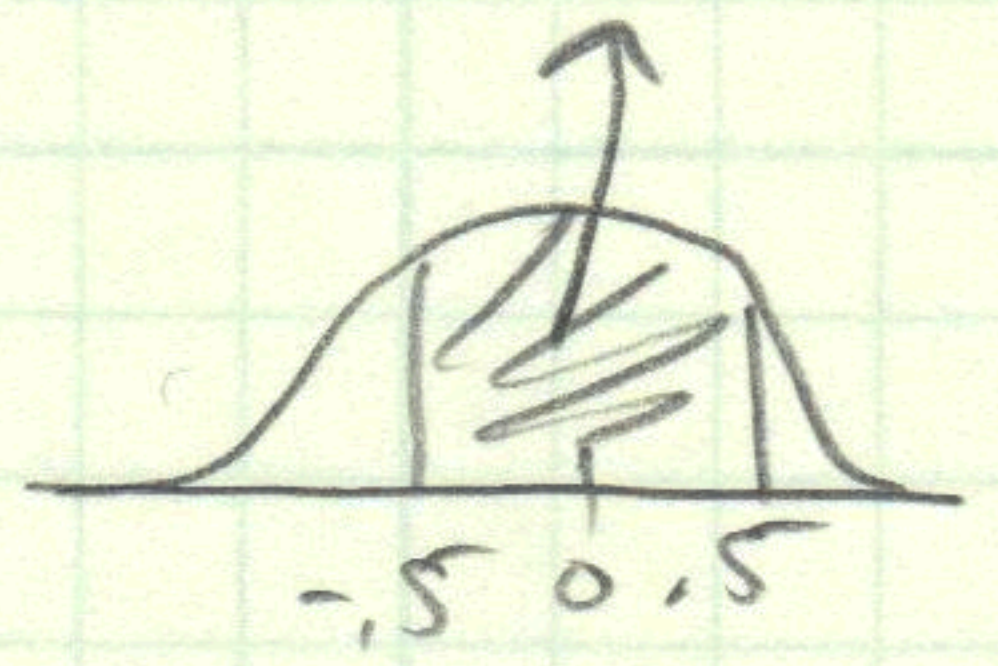
d- True



4e



$$\frac{33,000,000 - 33,300,000}{600,000} = -0.5 \approx 38.29$$



Middle  $\leftarrow$  Tail

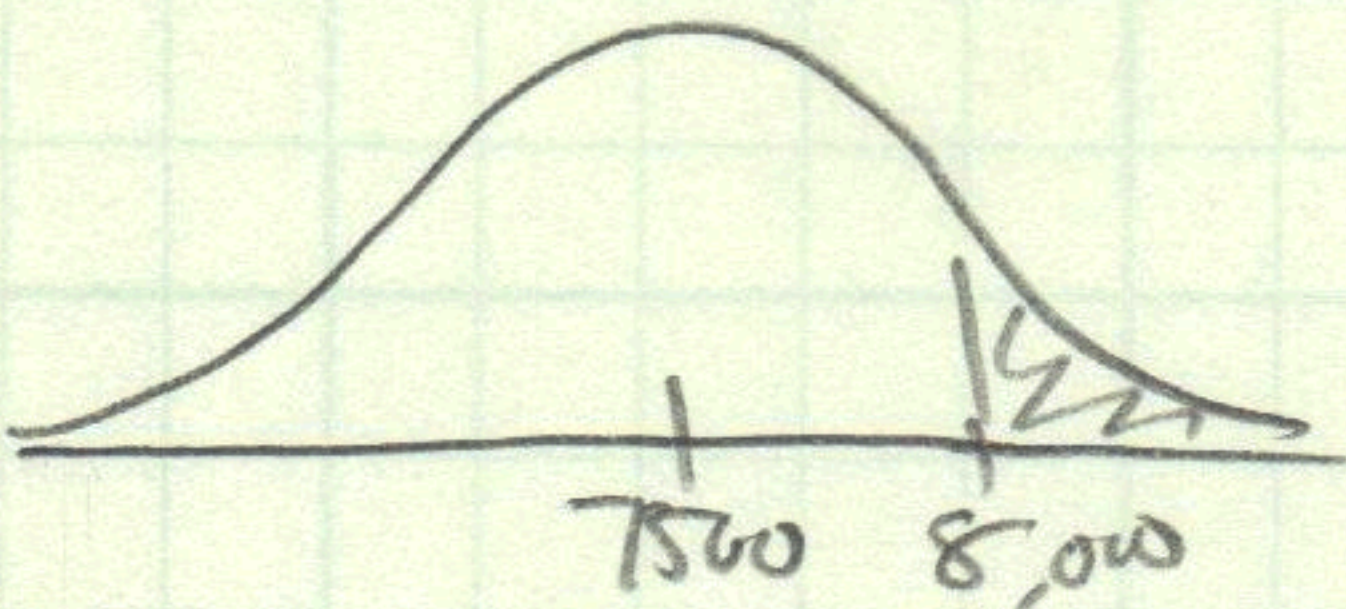
$$38.29 + \left( \frac{100 - 38.29}{2} \right) = \underline{69\%}$$

5 Total:

$$\begin{array}{|l} \text{box}_{\text{ave}} = 150 \\ \text{box}_{\text{SD}} = 35 \end{array} \quad \begin{array}{l} \updownarrow \\ 50 \end{array}$$

$$\begin{aligned} EV_{\text{sum}} &= 150 \times 50 = 7500 \\ SE_{\text{sum}} &= 35 \times \sqrt{50} = 247.5 \end{aligned}$$

$$4 \text{ tons} = 8,000 \text{ lbs}$$



$$\frac{8,000 - 7,500}{247.5} \approx 2 \approx 95\% \text{ Tail } \frac{100 - 95}{2} = \underline{2.5\%}$$

6 (ii) is right because .10% of 35,000,000 is bigger than .10% of 2,000,000.

7 a-True

b- False, the give or take is not appropriate when just talking about EV

c- True

d- False, chance error still exists.

e- True

f- False we know the box contents.

8 40% the EV%. Look at the Normal Curve.

9 Number of!

$$\begin{array}{l} \text{box}_{\text{ave}} = .33 \\ \text{box}_{\text{SD}} = .47 \end{array}$$

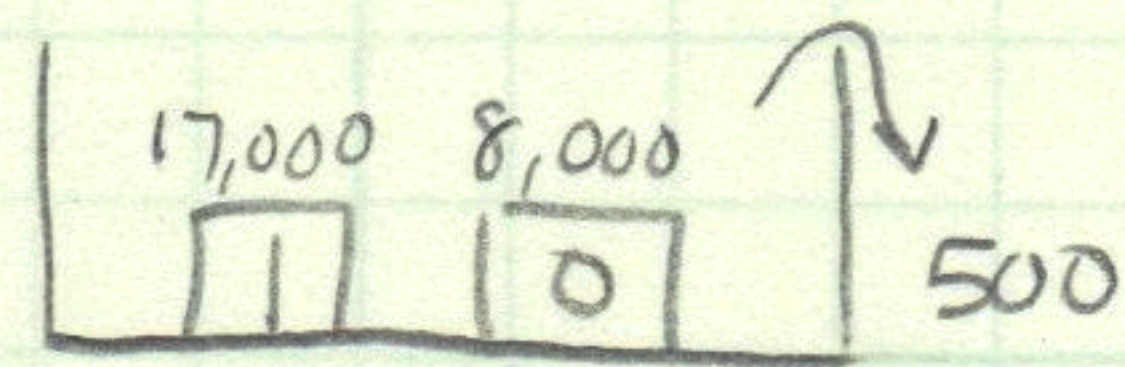
$$\begin{aligned} EV_{\text{sum}} &= .33 \times 600 = 200 \\ SE_{\text{sum}} &= .47 \times \sqrt{600} = 11.5 \end{aligned}$$

200 give or take 11.5 or so.



110 Yes. Keyword "Number of" find  $SE_{sum}$

11a  $357 = Obs.$   
 $340 = Exp.$



$box_{ave} = .68$

11b  $357/500 = 71.4\% = Obs$   
 $68\% = Exp.$

112 Total

$box_{ave} = 2.38$   
 $box_{sd} = 1.87$  } 400

$EV_{sum} = 2.38 \times 400 = 952$   
 $SE_{sum} = 1.87 \times \sqrt{400} = 37.4$

952 interviews, give or take 37.4 or so.